

SHEET 5

Exercise 1

Prove Fekete's Lemma.

Exercise 2

Let  $p < p_c$ . Prove that there exists  $c > 0$  s.t.

$$\forall x \in \mathbb{Z}^d \quad \frac{c}{\|x\|_\infty^{d(d-1)}} e^{-\frac{\|x\|_\infty}{\beta(r)}} \leq P_p[0 \leftrightarrow x] \leq e^{-\frac{\|x\|_\infty}{\beta(r)}}$$