## Algebraic Topology

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## Question 1:

Consider the cycle *a* given by the inclusion  $\partial \Delta^2 \to \Delta^2$ , and let *b* be its barycentric subdivision. Show explicitly that *a* and *b* differ by a relative boundary, i.e. write an element  $c \in \Delta_2(\Delta^2)$  such that  $\partial c - (a - b) \in \Delta_2(\partial \Delta^2)$ . You can present a solution by pictures.

## Question 2:

Let X be a topological space and Y be a subspace of X. Let  $i: Y \to X$  be the inclusion. Let C be space obtained from X by "attaching a cone on Y". More precisely, is the topological space

$$C = (Y \times [0,1]) \sqcup X / \sim$$

where  $\sim$  is defined as  $(y,0) \sim i(y)$  and  $(y,1) \sim (y',1)$  for all  $y, y' \in Y$ . Compute  $H_*(C)$ .

## Question 3:

Show that homotopy equivalence of chain complexes is an equivalence relation.