

For each of the following two questions, select *all* correct answers. There is at least one correct answer, and possibly more than one. A fully correct answer gives **one point**, if there is one mistake, it gives  $\frac{1}{2}$  *point*, and if there are two mistakes or more, it gives *zero point*.

- (1) Which of the following properties are true?
  - (a) The fundamental group of the Cantor space is trivial for any base point.
  - (b) The fundamental group of  $[0, 1] \times \mathbf{S}_1$  at  $(0, 1)$  is abelian.
  - (c) The fundamental group of  $[0, 1] \times \mathbf{S}_1$  at  $(0, 1)$  is trivial.
  - (d) The fundamental group of  $\mathbf{R}/\mathbf{Z} \times \mathbf{S}_1$  is isomorphic to  $\mathbf{Z}$ .
- (2) Which of the following maps are covering spaces?
  - (a) The map  $f: [0, 1] \times \mathbf{R} \rightarrow [0, 1]$  defined by  $f(x, y) = x$ .
  - (b) The map  $f: \mathbf{C} \rightarrow \mathbf{C}$  defined by  $f(z) = z^2$ .
  - (c) The map  $f: \mathbf{C}^* \rightarrow \mathbf{C}^*$  defined by  $f(z) = z^2$ , where  $\mathbf{C}^* = \mathbf{C} \setminus \{0\}$ .
  - (d) The map  $f: \mathbf{R} \rightarrow [-1, 1]$  defined by  $f(x) = \cos(x)$ .